YOSHIHIRO HORIHATA AND KEITA YOKOYAMA, Weak-Riemann mapping theorem and Picard's little theorem in weak second order arithmetic.
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In this research, we develop complex analysis within weak subsystems of second order arithmetic. We are mainly concerned with some versions of Riemann mapping theorem and Picard's theorem. It is known that basic parts of complex analysis can be developed within WKL<sub>0</sub> since Cauchy's integral theorem is equivalent to WKL<sub>0</sub>([1]). In [2], it is shown that the full version of Riemann mapping theorem is equivalent to ACA<sub>0</sub>. In this study, we show that the Riemann mapping theorem for polygonal region is provable in RCA<sub>0</sub>. Using this, we can prove Picard's little theorem within WKL<sub>0</sub>.

[1] YOSHIHIRO HORIHATA, KEITA YOKOYAMA, *Picard's little theorem in second order arithmetic*, preprint.

[2] KEITA YOKOYHAMA, Non-standard analysis in ACA<sub>0</sub> and Riemann mapping theorem, Mathematical Logic Quarterly, vol. 53 (2007), no. 2, pp. 132–146.